Calculations

Graphics

The following graphics are from the CalTester Paper Holden JP, Selbie WS, Stanhope SJ, “A proposed test to support the clinical movement analysis laboratory”.

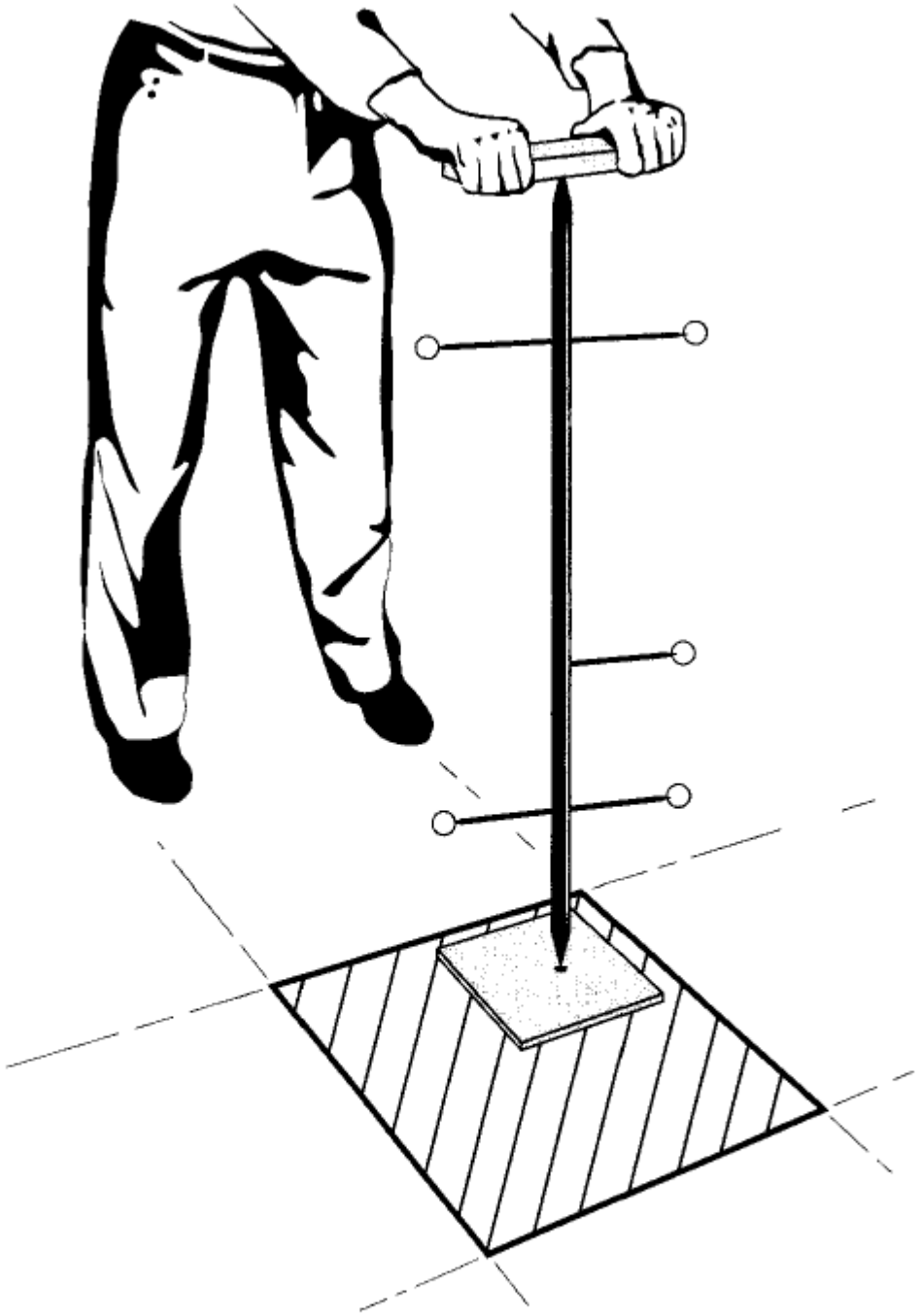


Fig. 1. A rigid mechanical device is used to apply forces to the FP. The device includes spherical, retroreflective targets attached to a machined rod having a pointed tip at each end. Using a hand held loading-bar and base-plate (shaded) with machined conical depressions, one can apply forces to the FP with a negligible applied moment. Data are sampled as the test device is manually loaded and slowly pivoted about the rod end on the base-plate.

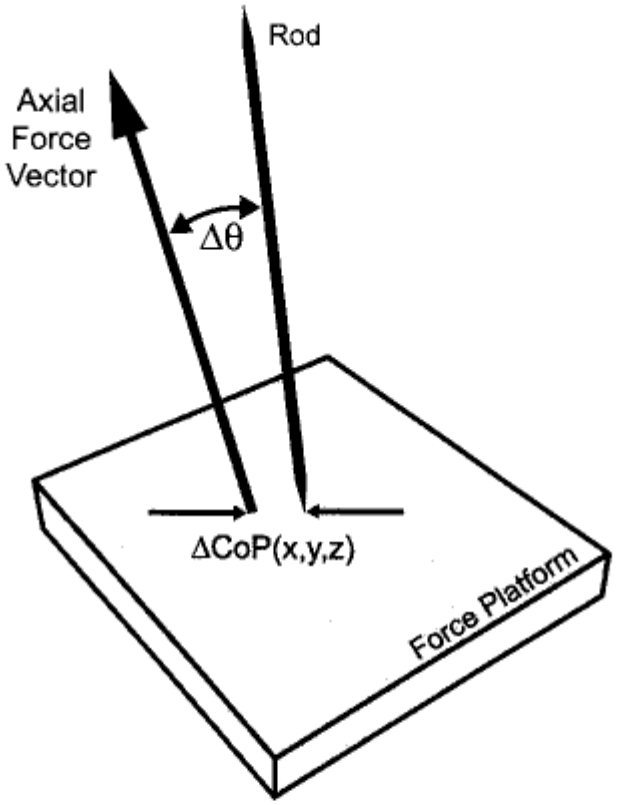


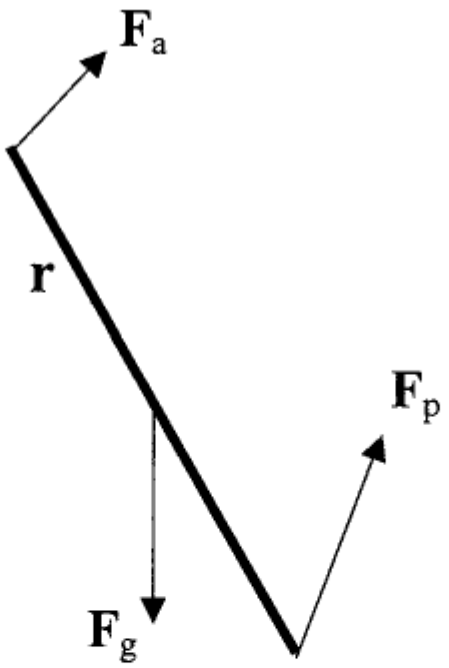
Fig. 2. The four test variables include: the rod orientation variable ($\Delta\theta$), the difference in spatial orientation (angle) of the rod as separately determined from FP measures (axial force vector) and kinematic measures of the rod (Appendix A, section I); and ΔCoP, the differences in the three coordinates of the CoP location, i.e. the x, y, and z components of the displacement vector between the CoP location determined from the FP and the tip of the testing rod as determined from the motion capture system.

Calculations

The following calculations and explanations are from the CalTester Paper Holden JP, Selbie WS, Stanhope SJ, “A proposed test to support the clinical movement analysis laboratory”.

Section I : Calculating the rod orientation variable under the assumed condition of static equilibrium

Free-body diagram of testing device: Fp, ground reaction force; Fg, gravitational force (weight); Fa, applied force; r, position vector between tips (p to a) of testing device rod:



$$\sum \mathbf{F} = 0 = \mathbf{F}_p + \mathbf{F}_a + \mathbf{F}_g \qquad (1)$$

$$\sum \mathbf{T}_p = 0 = \mathbf{r} \times \mathbf{F}_a + \frac{\mathbf{r}}{2} \times \mathbf{F}_g$$

$$= \mathbf{r} \times (-\mathbf{F}_p - \mathbf{F}_g) + \frac{\mathbf{r} \times \mathbf{F}_g}{2} \qquad (2)$$

$$\Rightarrow \mathbf{r}\left(-\mathbf{F}_p - \frac{1}{2}\,\mathbf{F}_g\right) = \mathbf{r} \times \mathbf{A} = 0 \qquad (3)$$

Thus, r and A are parallel and the test device rod orientation ® is defined entirely by the vector quantity A that is derived from FP measurements (Fp) and the physical characteristics of the testing device (Fg/2, i.e.the weight of the rod and its center of mass location; in this case, half the rod length).

$$\Delta\theta = \cos^{-1}\left(\hat{r} \cdot \hat{A}\right)$$

The rod orientation variable ($\Delta\theta$) is determined from the dot product of the unit vector along A and the unit vector aligned with the long axis of the rod ® as determined using the motion capture components.

Section II : Equation for evaluating the static equilibrium assumption

Under 2D dynamic conditions, the following holds:

$$|r \times A| = \left(\frac{mr^2}{4} + I_{cg}\right)\ddot{\theta} \qquad (4)$$

Rewriting the left-hand side of Eq. (4)

$$|r||A| \sin\beta = \left(\frac{mr^2}{4} + I_{cg}\right)\ddot{\theta}$$

Rearranging Eq. (5), the magnitude of the angular displacement (β) between vectors r and A due exclusively to the inertial terms can be isolated:

$$\beta = \sin^{-1}\left[\frac{\left(\frac{mr^2}{4} + I_{cg}\right)\ddot{\theta}}{|r||A|}\right] \qquad (6)$$

where r is the length of the testing device rod, Icg the moment of inertia of the test device rod about the center of mass location, m the mass of the testing device rod and $\ddot{\theta}$ is the angular acceleration of the testing device rod relative to an inertial reference frame.

CalTesterPlus does not calculate β since it operates under the assumption that there is no angular acceleration. For this reason it is important to move the CalTester rod slowly at a constant speed.

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